

Geovisualization

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Abstract

Geovisualization is primarily understood as the process of interactively visualizing geographic information in any of the steps in spatial analyses, even though it can also refer to the visual output (e.g., plots, maps, combinations of these), or the associated techniques. Rooted in cartography, geovisualization emerged as a research thrust with the leadership of MacEachren and colleagues when interactive maps and digitally-enabled exploratory data analysis led to a paradigm shift in 1980s and 1990s. A core argument for geovisualization is that visual thinking using maps is integral to the scientific process and hypothesis generation, and the role of maps grew beyond communicating the end results of an analysis or documentation process. As such, geovisualization interacts with a number of disciplines including cartography, visual analytics, information visualization, scientific visualization, statistics, computer science, art-and-design, and cognitive science; borrowing from and contributing to each. In this entry, we provide a definition and a brief history of geovisualization including its fundamental concepts, elaborate on its relationship to other disciplines, and briefly review the skills/tools that are relevant in working with geovisualization environments. We finish the entry with a list of learning objectives, instructional questions, and additional resources.

1. Definitions

- **Cartography**³: an influential conceptual model by MacEachren (1994) summarizing important dimensions in geovisualization (users, tasks, and interaction)
 - **user**: one of the dimensions in the Cartography³, characterizing user groups as public vs. expert
 - **task**: one of the dimensions in the Cartography³, referring to key concepts of exploration and communication
 - **interaction**: one of the dimensions in the Cartography³, referring to levels of interaction (low vs. high)
- **communication**: information transfer using a (visual) language
- **confirmation**: once a hypothesis is formed, using statistical methods to analyze and confirm the observed relationships in the data

- ***cognitive walkthrough***: a process in usability evaluation in which a set of questions from the perspective of the user is asked and answered by the team conducting the usability study
- ***exploration***: the process of examining a dataset in a systematic manner through summarizing, plotting and conducting statistical analyses with the intention to arrive at insights and hypotheses
- ***geovisualization***: visualization of geographic information (spatial, temporal, or attribute, or a combination of all three), the process of creating interactive visualizations for geographic analysis, using maps, map-like displays, multimedia, plots and graphs (also in combination) to aid visual thinking and insight/hypotheses generation, and a perspective on cartography
- ***hypothesis***: a proposition based on informed reasoning with limited evidence, to be followed by systematic scientific investigation
- ***insight***: a comprehensive grasp and a clear understanding of something
- ***presentation***: showing and disseminating the synthesized findings
- ***Swoopy***: a conceptual model proposed by DiBiase (1990) defining geovisualization as a process that facilitates thinking
- ***synthesis***: a meaningful combination of multiple perspectives about (geographic) phenomena from multiple analyses, generalizing confirmed findings where possible
- ***visual thinking***: thinking in images, or generating ideas/insights with the help of images
- ***visualization***: forming a mental image; displaying data using computer generated imagery; the process of making something visible to mind

2. Description

Geovisualization is an elusive word to define. The term is used inconsistently, referring to a map, a display type, a process, a technique, a way of using maps, and an academic discipline. Despite this inconsistency, the context in which the term geovisualization appears almost always has relationship to interactive digital cartography. As computers dominated almost all domains of scholarly work (and human life), a need to distinguish *computer cartography* from the thousands of years old art and science of *traditional cartography* has emerged. This need was fueled by the fact that the digital/dynamic displays offer remarkably more flexibility and new opportunities for the design and use of maps in comparison to static media, and that the questions we can ask and answer with maps and map-like displays have changed with computers. These developments caused a paradigm shift from ***communication*** in cartography with a focus on explanatory approaches (see **Cartography & Science**), to ***exploration*** and knowledge construction in geovisualization (MacEachren 1994). The fact that today a user can make on-demand changes to the display and access a variety of linked visualizations in real time (and thus explore the data from different perspectives) situates geovisualization at the core of visual information processing to

facilitate thinking in complex decision-making tasks and in scientific investigations (Andrienko et al., 2014). A geovisualization environment still enables visual communication, but importantly, one can visualize the data also at early- and mid-stages of the knowledge construction process in spatial analysis, and generate hypotheses based on the insights prompted by the visual stimuli. This line of thinking was affected by developments in statistics, specifically, moving from explanatory analyses to the *exploratory data analysis* (EDA) (Tukey, 1977). According to Google's online ngrams tool (<https://books.google.com/ngrams>, Michel et al., 2011); the term geovisualization starts frequently appearing in textbooks around 1990s, and slowly replaces *digital cartography* and *computer cartography* (Çöltekin et al., 2017) (see **Cartography & Technology**). This timing coincides with seminal publications in *scientific* and *information visualization* domains (McCormick 1987; Robertson et al. 1989), likely driven by the progress in technology, and especially in computer graphics, and draws from the developments in these domains.

2.1. Geovisualization concepts

Along with a plethora of technology-driven developments, important conceptual frameworks also were proposed around 1990s. A defining theoretical framework on geovisualization is MacEachren's (1994) *Cartography*³ (Figure 1 right, and Figure 2, also see MacEachren et al., 2004). MacEachren's framework extends the earlier *Swoopy* framework proposed by DiBiase (1990). DiBiase's Swoopy framework offers a continuum in which we see both *visual thinking* and *visual communication*, and as such, it provides foundations as to how we think about geovisualization today (Figure 1 left).

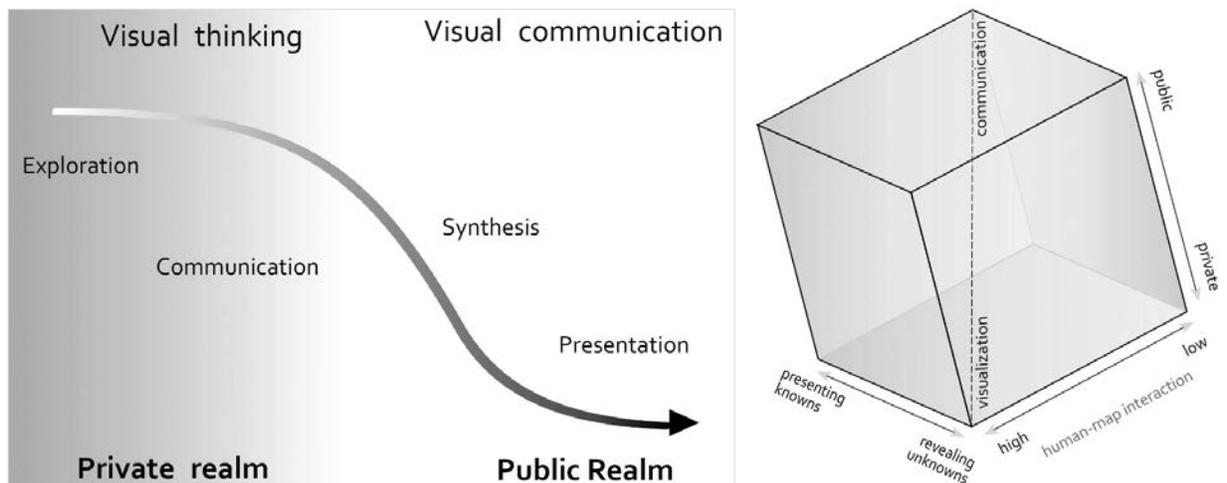


Figure 1. Left: DiBiase's (1990) "Swoopy". Right: MacEachren's (1994) *Cartography*³ conceptualization of geovisualization on tasks, users, and interaction types as dimensions (figure redrawn from Robinson, 2017, original artwork courtesy of Anthony Robinson).

The Cartography³ framework extends the Swoopy framework, essentially adding the *interaction* (low vs. high) as a dimension and mapping its relationship to *users* (public vs. expert), and *tasks* (communication vs. exploration), in a continuum (Figure 1, right). MacEachren et al. (2004) further developed the Cartography³ later (Figure 2), slightly adjusting Swoopy's 'idealized' research steps *exploration*, *confirmation*, *synthesis*, and *presentation* (Figure 1 left) by replacing *confirmation* step with *analysis*.

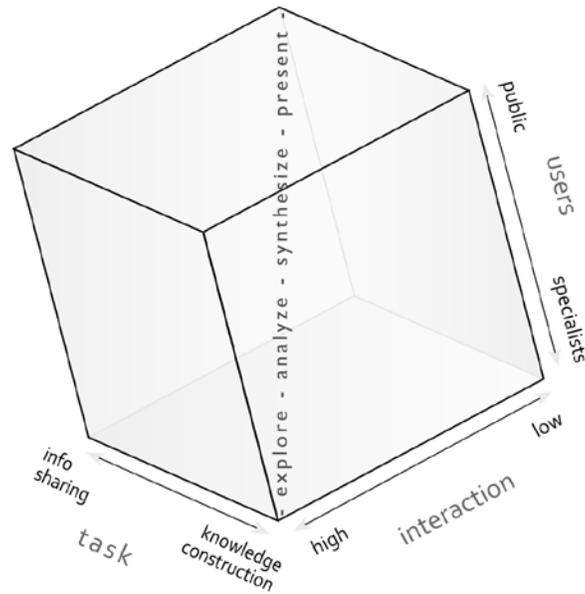


Figure 2. An update to Cartography³, 10 years after its conception (figure redrawn from MacEachren, 2004, original artwork courtesy of Alan MacEachren).

The updated framework (Figure 2) sums up the core functions of geovisualization: With the support from geovisualization software environments, the public (e.g., non-expert users) or specialists (e.g., researchers, decision makers) can discover patterns and form informed questions (exploration), conduct analyses to confirm or reject individual hypotheses (analysis/confirmation), generalize the findings (synthesis), and present/communicate these findings. The framework suggests that the specialists use (more) interactive geovisualization environments in exploratory processes for knowledge construction, whereas interaction requirements are lower as we move towards the goal to communicate (info sharing/presentation) with/by public. The concepts covered by Cartography³—and its 2004 update—remain relevant today and are core to our understanding of how geovisualization was born as a perspective on cartography.

Coherent with its history within the cartography community, the use of the term geovisualization have become commonplace in geographic information science (GIScience) and related fields after the International Cartographic Association's (ICA) *Commission on Visualization and Virtual Environments*

was established by Alan MacEachren and Menno-Jan Kraak in 1995. Note that the commission changed its name to *Commission on GeoVisualization* (<http://geoanalytics.net/ica/>) in the following terms, and to *Visual Analytics* in 2015 (<http://viz.icaci.org/>).

2.2. Scholarly influences and interdisciplinary interactions

As indicated with the commission name-change mentioned above, an important influential development related to geovisualization is the emergence of the sister discipline *visual analytics* (Thomas & Cook 2005). Soon after the phrase ‘visual analytics’ was coined, it rapidly attracted an active interdisciplinary community, where the goal was to combine the strengths of humans and machines into one ‘dashboard’ to support analytical reasoning (see **Geovisual Analytics**). Geovisual analytics differs from geovisualization mainly in its explicit inclusion of computational methods. However, studying perceptual and cognitive abilities of humans in visuospatial sense- and decision-making is an overlapping interest between geovisualization and geovisual analytics domains. Understanding human visuospatial information processing mechanisms can guide design of visuospatial displays and visualization software environments, thereby reducing cognitive load and enhancing user performance with geospatial displays by assisting in situations where the human cognitive capacity might fall short (Hegarty, 2009).

Besides cartography and geovisual analytics, geovisualization naturally shares goals and methods with *information* and *scientific visualization* domains (*Infovis* and *Scivis*). The boundaries between Infovis and Scivis (and Geovis) are not crisp, and can be imagined as a continuum. One can also argue that they all do “data visualization”. Infovis often (but not exclusively) deals with visual or spatial metaphors for non-visuospatial data (i.e., data that contains no inherent spatial structure), and features abstract visualizations (Robertson et al., 1991); while Scivis is often (again, not exclusively) concerned with documenting (sometimes invisible) processes and phenomena, which have inherent spatial structures (McCormick et al., 1987).

Geographic information and phenomena can be visualized on many different display types, including in immersive virtual and augmented reality environments. In relation to virtual environments, an influential concept is *the Digital Earth*, a digital replica of the world captured in all its complex detail (Gore, 1998), which led to the development and immense popularization of the digital globes. A more in-depth coverage of the Digital Earth concept, and virtual/augmented reality displays, is beyond the scope of this section, nevertheless it is important to note that they are important drivers in both technological and conceptual developments related to geovisualization (see **Virtual & Immersive Environments**).

3. Geovisualization environments

When we consider what ‘geographic visualization’ means purely based on natural language—as opposed to framing it as a term with the historical development as summarized above—the word geovisualization can refer to a very broad range of visual outputs (e.g., products such as maps and similar, besides the processes). Even though widely used as such, different to a map or a map-like visuospatial display, geovisualization is rather concerned about the *use* than *design*. Nonetheless, a geovisualization environment is usually a software environment that, by definition, must include visual outputs such as maps, map-like displays (e.g., satellite imagery), media that contain visuospatial information (e.g., street level imagery, 3D models, videos, animations, etc.), plots, charts, and other types of graphics. These visual media are shown in ‘multiple linked views’ where possible through brushing, linking and highlighting mechanisms in almost all geovisualization software (e.g., Figure 3, Table 1).

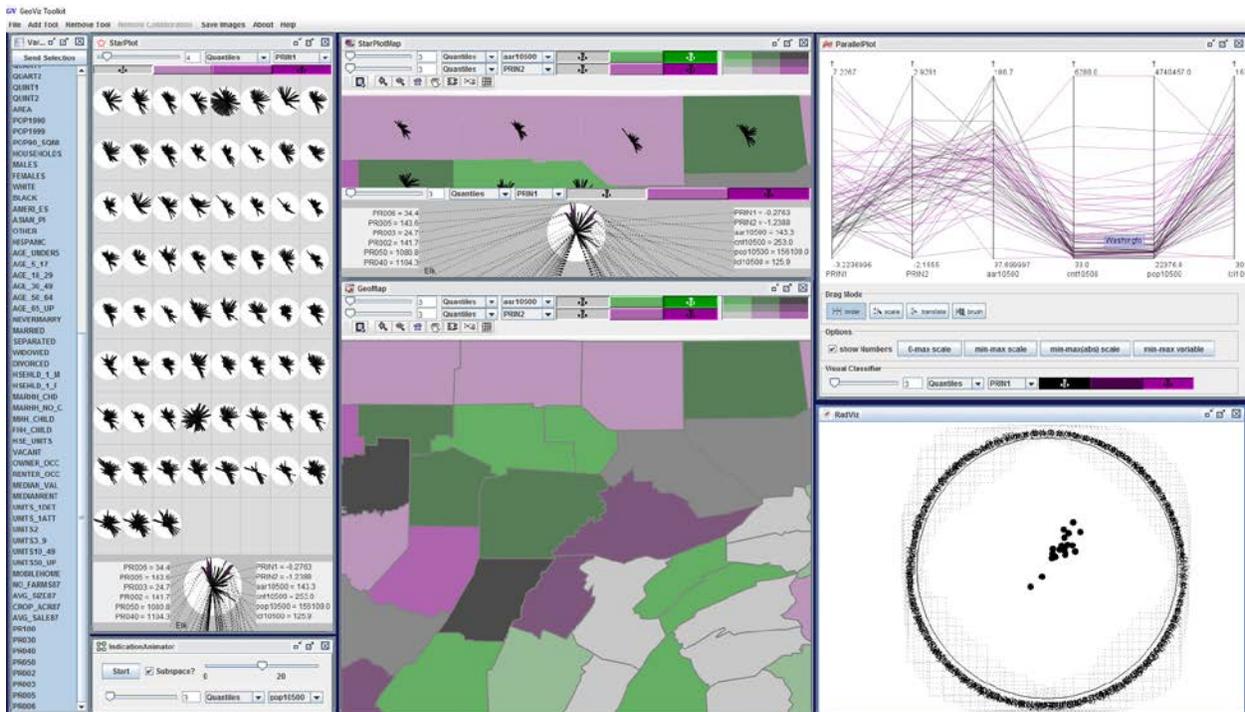


Figure 3. Screenshot produced from GeoViz Toolkit, a dedicated geovisualization software by Frank Hardisty, Aaron Myers, and Ke Liao (<https://www.geovista.psu.edu/geoviztoolkit/>). The interface is modular, i.e., different display types can be added or removed, and the views are linked.

Table 1. An overview of (selected) influential geovisualization software (adapted from Robinson, 2017).

Software	Release date	Team	Key features
GeoVISTA Studio	Late 1990s	Takatsuka and Gahegan 2002	Multiple linked views, animation, interactive, component-by-component reconfiguration, user-driven highlighting
CommonGIS (a.k.a. V-Analytics)	Late 1990s	Andrienko, Andrienko, and Voss 2005	Multiple linked views, animation, interactive, exploration of attributes, dynamic manipulation of query parameters
GeoViz Toolkit	Late 2000s	Hardisty and Robinson 2011	Multiple linked views, animation, interactive, integration to World Wide Web
GeoAnalytics Visualization (GAV) Toolkit (OECD eXplorer)	Late 2000s	Jern et al. 2007	Multiple linked views, animation, interactive, integration to World Wide Web
...			

Some of the influential geovisualization software/toolkits are listed for reference in Table 1. Availability, (and importantly, usability) of such off-the-shelf software plays an important role in the spread of geovisualization and its adaptation for real-life knowledge construction and decision making situations.

3.1. Skills relevant in geovisualization

Modern tools allow creating interactive visual displays fairly quickly and without a very steep learning curve (e.g., GeoVISTA Studio, Google Maps, Scribble Maps, Mapbox, Carto...), and there are fully flexible software development environments and scripting languages for visual programming (e.g., Processing, Python, D3.js, Leaflet, WebGL...). Whether we use software to prepare the visual output or program it ourselves, the very first skill we need is a good understanding of what the *data preprocessing* involves for the project's needs. Consequently, the data domain, erroneous data, and the data distributions should be examined first, which require statistics skills and experience in data handling. If the data is not preprocessed properly, in exploratory analyses, the resulting visual output might lead to wrong insights (thus resulting hypotheses might be misguided), or if the goal is to communicate, the output will fail to convey the intended message. Such threats should be assessed both by reflection on the statistical data processing, and in user studies (see **Usability Engineering**).

Given the ever-growing data collection opportunities (e.g., with new sensors, mobile phones, social media), raw data often contain more data items than we are able to visualize effectively. This issue

requires a good understanding of available visualization techniques and display design considerations (e.g., Hegarty et al., 2009). For example, although there are space-efficient visualization techniques (e.g., treemaps, pixel maps, cartograms), visualizing the raw data ‘as is’ often results in cluttered displays and overplotting, causing the so-called “hairball effect” (Buchmüller et al., 2015). Against the hairball effect, geovisualization displays often represent aggregated or clustered data highlighting only the ‘interesting aspects’ in the (vast amounts of) data (see **Big Data Visualization**). Deciding what aspects are interesting can be left to the user to explore in an interactive environment with careful interface design, which is ideally user-tested for the intended user group.

The transformation from the data space to the visualization space requires a thorough understanding of the implications of design on the successful use of the resulting visual displays (see **Aesthetics and Design, User Interface and User Experience (UI/UX) Design, Usability Engineering**). For example, an understanding of when and how to employ different visual variables (see **Symbolization & the Visual Variables**), and the relevant perceptual and cognitive processes are important. Design-related knowledge will ensure that the visual encoding always reflects the documented (or at least anticipated) requirements of the target user group. It is important to remember that there are large individual and group differences among users (Griffin et al., 2017). Note that testing the visual displays on oneself is not a predictor of how successfully the others are able to work with these displays. Also importantly, because most geovisualization environments are interactive, in addition to display design, understanding interaction paradigms and interface design is necessary to increase their potential usability and usefulness (see **User Interface and User Experience (UI/UX) Design**). Last but not least, the more the relevant technology (e.g., software, scripting or programming language) is mastered, the more flexibility the designer will have in implementing and experimenting with what they have in mind.

3.2. Reading and interpreting graphics

Besides the necessary technology and design skills discussed above, *graphical* or *visual literacy* (Dondis, 1974) is of core importance to visual thinking, and therefore, necessary to read and interpret visuospatial displays. To benefit from geovisualization environments, users need to be aware of their level of experience as well as their perceptual and cognitive limitations (Slocum et al., 2009; Hegarty et al., 2009). Similarly, it is important to be informed about a number of *cognitive biases* (Tversky & Kahneman, 1974) that may be relevant in the process of working with geovisualization environments. The *confirmation bias*, for example, might (mis)guide the attention to verify hypotheses made before exploring data. Additionally, the complexity of data or the represented phenomena might impose limitations on the legibility and expressiveness of a visuospatial display. For example, if the display shows aggregated data,

one must pay close attention to the aggregation unit when interpreting (e.g., election results will look different at city vs. state levels), and be aware of modifiable areal unit problem (MAUP, Openshaw, 1984). Another well-known issue is the distortions introduced to maps by map projections, which might lead to miscalculations and misinterpretations (Battersby & Montello, 2009; see also **Map Projections**). Educating oneself on issues with visuospatial displays and maps is important to avoid generating naïve hypotheses when working with a geovisualization environment. In other words, the mental uncompressing and interpretation of multiple-linked-view visualization environments requires ‘sanity checks’ to verify what is shown. It is always a good idea to compare one’s interpretations of the visual displays with facts from other sources, and check if alternative displays of the same data might paint a different picture.

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Additional Resources:

Books, book chapters, journal articles:

Dodge, M., McDerby, M., & Turner, M. (Eds.). (2011). *Geographic visualization: Concepts, tools and applications*. John Wiley & Sons.

Dykes, J., MacEachren, A. M., & Kraak, M. J. (2005). *Exploring geovisualization*. Elsevier.

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<https://www.tandfonline.com/toc/tcag20/28/1?nav=toCList>

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Ward, M. O., Grinstein, G., & Keim, D. (2010). Visualization Techniques for Geospatial Data. In: *Interactive data visualization: foundations, techniques, and applications*. CRC Press.

Online resources:

International Cartographic Association (ICA) commissions

Commission on Visualization and Virtual Environments (1995-2007)

https://icaci.org/files/documents/commissions/reports_2007/VisualizationAndVirtualEnvironments_07.pdf

Commission on GeoVisualization (2007-2015) <http://geoanalytics.net/ica/>

Commission on Geovisual Analytics (2015- ...) <http://viz.icaci.org/>

[Buczowski, A. \(2016\) Top 19 geovisualization tools, APIs and libraries that will let you create beautiful web maps: http://geoawesomeness.com/top-19-online-geovisualization-tools-apis-libraries-beautiful-maps/](http://geoawesomeness.com/top-19-online-geovisualization-tools-apis-libraries-beautiful-maps/)

An online selection of cartography/geovis tools: <http://cartography.oregonstate.edu/software.html>

An online selection of data visualization tools <http://selection.datavisualization.ch/>

Learning objectives

- Understand how geovisualization is defined, differentiate between the different ways in which the term geovisualization is used
- Identify the characteristics of geovisualization as a process, and relate these characteristics to modern day mapping systems and map use
- Understand the relevant abilities, skills, and literacy in successfully working with geovisualization environments
- Use a geovisualization application to explore a geospatial dataset. Note the geographic insights you find and hypotheses worth pursuing with additional analysis and visualization

Instructional Questions:

- Imagine that you want to show global migration patterns over time for an online newspaper for an interactive story aimed at public.
 - According to the Cartography³'s three dimensions, what are the main considerations in this project?
 - What are the steps in creating an interactive geovisualization in such a project?
 - What procedures must one follow to ensure that the proposed visualization solution functions as intended?
 - What tools would be most appropriate in creating such a geovisualization display, and why?
- Create a scenario similar to the one described above where a geographic phenomenon needs to be visualized for a *specific user group*. You can choose any user group, that you can define e.g., people of certain age (children or older adults), people who cannot read, have serious vision problems, people who need to get around in wheelchairs, etc. How would you optimize the design for the user group you have in mind? Based on a cognitive walkthrough, list hypothetical user requirements, relevant user characteristics, and create a (mockup) geovisualization that meets these requirements. Justify your choices.
- Write an essay to respond to the following question: What are the three important scientific and conceptual developments that influenced the development of geovisualization, and in which way these have been influential? Illustrate your arguments with examples.
- Using the Cartography³ framework (as shown on the right), indicate the approximate position of the following maps/interfaces (shown in class) along the *communication* ↔ *visualization* axis: (a) Outputs from Tableau, New York Times or similar (choose one), (b) Your Campus Map, and (c) ArcGIS (screenshots of the maps/interfaces will be provided by your instructor, if you're doing the exercise on your own, select three that you are familiar with). Describe why each map fits into the selected location in the cube. Then, provide one example of an interactive map we discussed in lecture that you feel does not fall cleanly along the *communication* ↔ *visualization* axis, and place this confounding interactive in the Cartography³ diagram. Justify why it fails to align with this framework, based on the three axes that define the cube space.

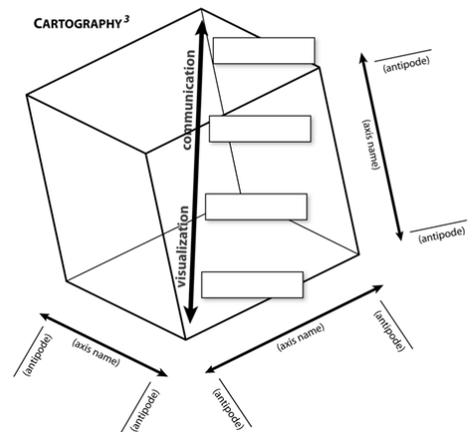


Image: Courtesy of Robert Roth